

1. Factor completely each of the following expressions...

[8]

a)  $15x^3 + 16x^2 - x - 2$

b)  $512a^{27} - b^9$

2. Divide:

$$(5x^5 - 2x^3 + x - 6) \div (x^2 - 1)$$

[4]

3. Determine a polynomial equation that has the following roots:  $x = \frac{1}{4}, \frac{-2 \pm 2\sqrt{3}}{5}$  [5]

4. Solve the following polynomial equation...  $3 + 3x^2(3x + 2) = (x + 5)^2 + 2(x^2 - 10)$  [5]

5. Expand the following using the binomial theorem:  $(-3x^6 + 5y^4)^4$  [5]

6. Given that the binomial expression  $(2x^{10} - 3y^7)^{14}$  is expanded, determine the numerical coefficient of the term that would have the variable part  $x^{60}y^{56}$ . [3]

7. When the polynomial  $-2px^3 + 3x^2 + 2kx + 1$  is divided by the binomial  $x + 2$  the remainder is 5, and when divided by the binomial  $x - 1$  the remainder is 2. Determine the values of  $p$  and  $k$ . [6]

8. Solve the following:  $6^{x^3}(6^{5x}) = 36^{2x^2+1}$  [4]